

Booklet of Figures
for
STAC33 Final Exam

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```

library(MASS)
library(tidyverse)

## -- Attaching packages -----
## v ggplot2 3.3.3    v purrr  0.3.4
## v tibble  3.1.5    v dplyr  1.0.8
## v tidyr   1.1.2    v stringr 1.4.0
## v readr   2.0.1    v forcats 0.5.1
## -- Conflicts -----
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()    masks stats::lag()
## x dplyr::select() masks MASS::select()

library(smmr)
library(PMCMRplus)
library(broom)
library(cmdstanr)

## This is cmdstanr version 0.4.0
## - Online documentation and vignettes at mc-stan.org/cmdstanr
## - CmdStan path set to: /home/ken/.cmdstanr/cmdstan-2.26.1
## - Use set_cmdstan_path() to change the path
##
## A newer version of CmdStan is available. See
?install_cmdstan() to install it.
## To disable this check set option or environment variable
CMDSTANR_NO_VER_CHECK=TRUE.

```

Figure 1: Packages

```

Ni:Current
19.1:0.095
38.2:0.174
57.3:0.256
76.2:0.348
95:0.429
114:0.500
131:0.580
150:0.651
170:0.722

```

Figure 2: Nickel data

##	state	sex	diag	death	status	T.categ	age
## 1	NSW	M	1989-11-09	1990-05-04	D	hs	35
## 2	NSW	M	1990-03-13	1990-05-19	D	hs	53
## 3	NSW	M	1986-02-24	1987-05-02	D	hs	42
## 4	NSW	M	1986-03-22	1986-06-07	D	haem	44
## 5	NSW	M	1987-06-03	1988-03-04	D	hs	39
## 6	NSW	M	1987-04-20	1988-04-27	D	hs	36
## 7	NSW	M	1989-06-03	1990-06-27	D	other	36
## 8	NSW	M	1987-06-30	1990-04-22	D	hs	31
## 9	NSW	M	1988-08-25	1989-12-30	D	hs	26
## 10	NSW	M	1988-07-31	1989-10-08	D	hsid	27
## 11	NSW	M	1988-07-08	1988-07-24	D	hs	45
## 12	NSW	M	1987-12-21	1988-10-24	D	hs	36
## 13	NSW	M	1988-06-07	1988-09-07	D	hs	27
## 14	NSW	M	1988-05-19	1989-02-08	D	hs	35
## 15	NSW	M	1988-08-13	1991-07-01	A	hs	30
## 16	NSW	M	1988-11-21	1989-04-02	D	hs	39
## 17	NSW	M	1989-03-22	1990-08-31	D	hs	30
## 18	NSW	M	1989-11-27	1991-07-01	A	haem	21
## 19	NSW	M	1990-02-05	1991-07-01	A	hs	56
## 20	NSW	M	1990-03-04	1990-08-02	D	hs	41

Figure 3: Australian AIDS data, some

```

river_water

## # A tibble: 5 x 2
##   upstream downstream
##   <dbl>         <dbl>
## 1     4.8           5
## 2     5.2          4.7
## 3     5            4.9
## 4     4.9          4.8
## 5     5.1          4.9

```

Figure 4: River water data

```

with(river_water, t.test(upstream, downstream, alternative = "less",
                          paired = TRUE))

##
## Paired t-test
##
## data: upstream and downstream
## t = 1.2472, df = 4, p-value = 0.8598
## alternative hypothesis: true difference in means is less than 0
## 95 percent confidence interval:
##      -Inf 0.3792992
## sample estimates:
## mean of the differences
##                0.14

```

Figure 5: River water data analysis 1

```

t.test(oxygen~where, alternative = "less", data = river2)

##
## Welch Two Sample t-test
##
## data: oxygen by where
## t = -1.6059, df = 7.2746, p-value = 0.07536
## alternative hypothesis: true difference in means is less than 0
## 95 percent confidence interval:
##      -Inf 0.02423248
## sample estimates:
## mean in group downstream    mean in group upstream
##                4.86                5.00

```

Figure 6: River water data analysis 2

```

t.test(oxygen~where, alternative = "less", var.equal = TRUE,
      data = river2)

##
## Two Sample t-test
##
## data: oxygen by where
## t = -1.6059, df = 8, p-value = 0.07348
## alternative hypothesis: true difference in means is less than 0
## 95 percent confidence interval:
##      -Inf 0.02211164
## sample estimates:
## mean in group downstream    mean in group upstream
##                4.86                5.00

```

Figure 7: River water data analysis 3

```

median_test(river2, oxygen, where)

## $table
##           above
## group      above below
## downstream    1     2
## upstream      3     1
##
## $test
## what      value
## 1 statistic 1.2152778
## 2          df 1.0000000
## 3 P-value 0.2702894

0.2703/2

## [1] 0.13515

```

Figure 8: River water data analysis 4

```
d1

## # A tibble: 2 x 3
##   x     y     z
##   <dbl> <dbl> <dbl>
## 1    10    11    13
## 2     9    12    14
```

Figure 9: Dataframe d1

```
d2

## # A tibble: 2 x 4
##   x     y_first y_second y_third
##   <chr>   <dbl>   <dbl>   <dbl>
## 1 a         10       11       13
## 2 b         12       15       16
```

Figure 10: Dataframe d2

```
d3

## # A tibble: 4 x 3
##   id x     y
##   <dbl> <chr> <dbl>
## 1     1 a     10
## 2     2 a     11
## 3     1 b     12
## 4     2 b     13
```

Figure 11: Dataframe d3

```
d4

## # A tibble: 4 x 3
##   x     y     z
##   <chr> <chr> <dbl>
## 1 a     b     9
## 2 c     d    10
## 3 a     d    11
## 4 c     b    12
```

Figure 12: Dataframe d4

```

## Rows: 414 Columns: 8-- Column specification -----
## Delimiter: ","
## dbl (8): No, X1 transaction date, X2 house age, X3 distance to
the nearest M...
## i Use `spec()` to retrieve the full column specification for
this data.
## i Specify the column types or set `show_col_types = FALSE` to
quiet this message.

## # A tibble: 414 x 5
##   sale_date   age    mrt  conv price
##   <dbl> <dbl> <dbl> <dbl> <dbl>
## 1  2013.    32   84.9    10  37.9
## 2  2013.   19.5  307.     9  42.2
## 3  2014.   13.3  562.     5  47.3
## 4  2014.   13.3  562.     5  54.8
## 5  2013.     5   391.     5  43.1
## 6  2013.    7.1 2175.     3  32.1
## 7  2013.   34.5  623.     7  40.3
## 8  2013.   20.3  288.     6  46.7
## 9  2014.   31.7 5512.     1  18.8
## 10 2013.   17.9 1783.     3  22.1
## # ... with 404 more rows

```

Figure 13: Taiwan house data (some)


```
boxcox(price ~ sale_date + age + mrt + conv, data = houses)
```

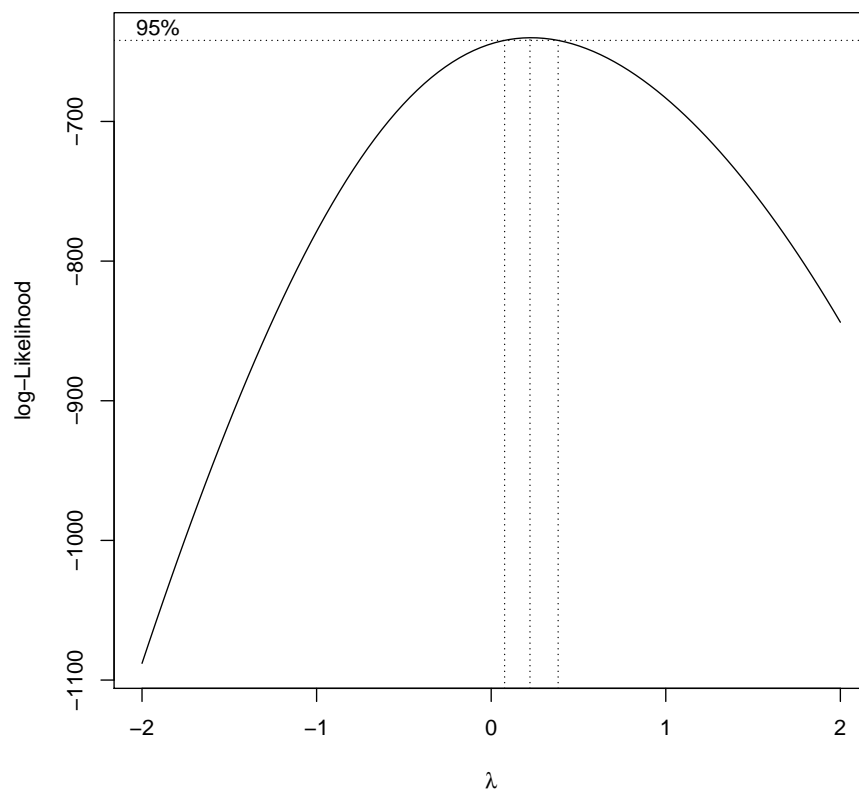


Figure 14: Taiwan houses Box-Cox analysis

```

houses.1 <- lm(log(price) ~ sale_date + age + mrt + conv, data = houses)
summary(houses.1)

##
## Call:
## lm(formula = log(price) ~ sale_date + age + mrt + conv, data = houses)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -1.77830 -0.11950 -0.00312  0.12172  1.06692
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -3.146e+02  8.268e+01  -3.806 0.000163 ***
## sale_date    1.582e-01  4.107e-02   3.851 0.000136 ***
## age          -6.459e-03  1.017e-03  -6.353 5.62e-10 ***
## mrt          -1.898e-04  1.152e-05 -16.470 < 2e-16 ***
## conv         3.189e-02  4.933e-03   6.465 2.88e-10 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 0.2345 on 409 degrees of freedom
## Multiple R-squared:  0.6465, Adjusted R-squared:  0.643
## F-statistic: 187 on 4 and 409 DF, p-value: < 2.2e-16

```

Figure 15: Taiwan houses regression analysis

```
ggplot(houses.1, aes(x = .fitted, y = .resid)) + geom_point()
```

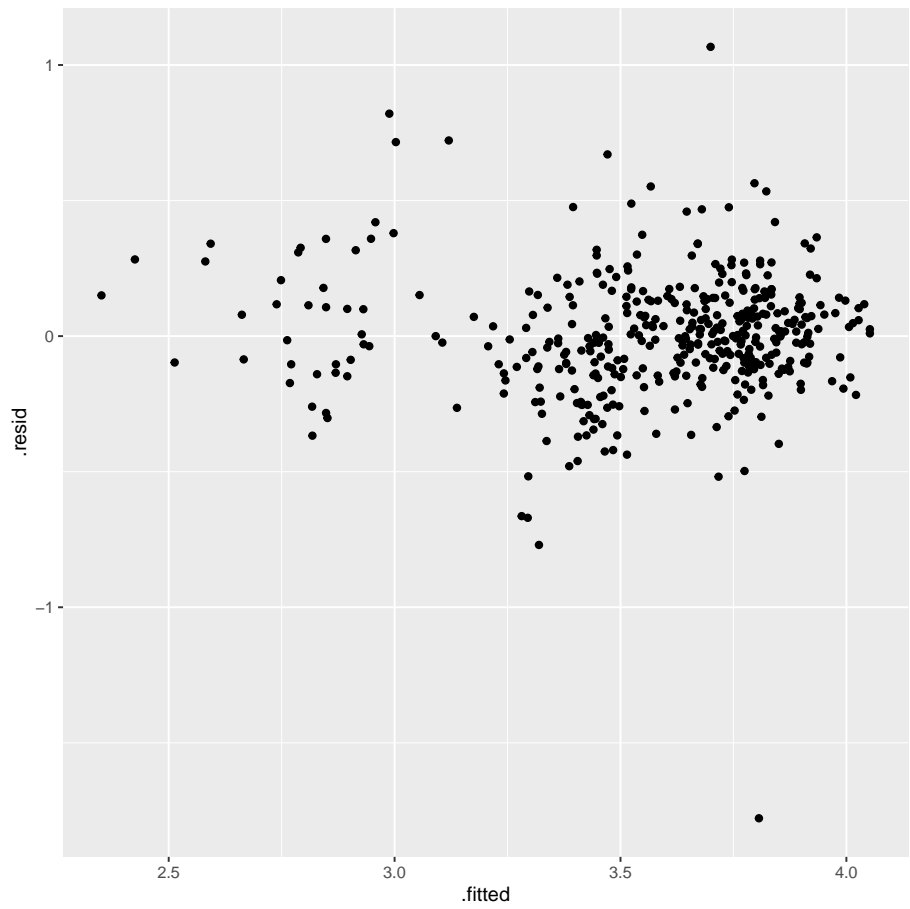


Figure 16: Taiwan houses residual plot 1

```
ggplot(houses.1, aes(sample = .resid)) + stat_qq() + stat_qq_line()
```

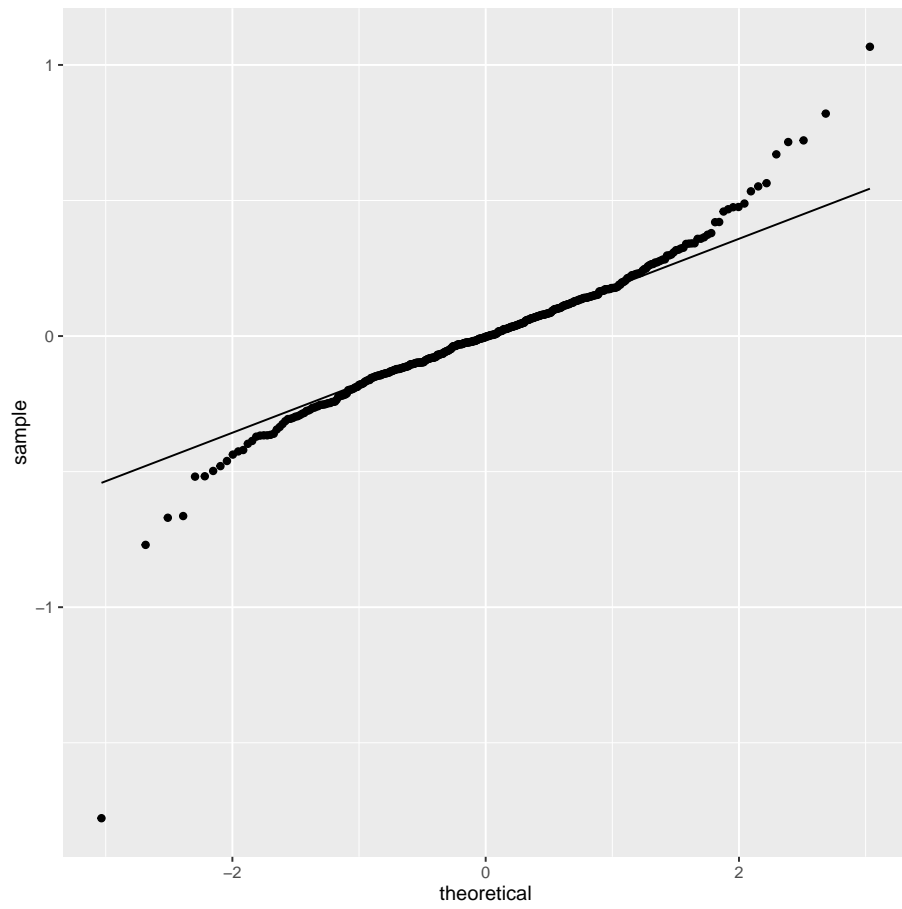


Figure 17: Taiwan houses residual plot 2

```
houses.1 %>% augment(houses) %>%
  pivot_longer(sale_date:conv) %>%
  ggplot(aes(x = value, y = .resid)) + geom_point() +
  facet_wrap(~name, scales = "free")
```

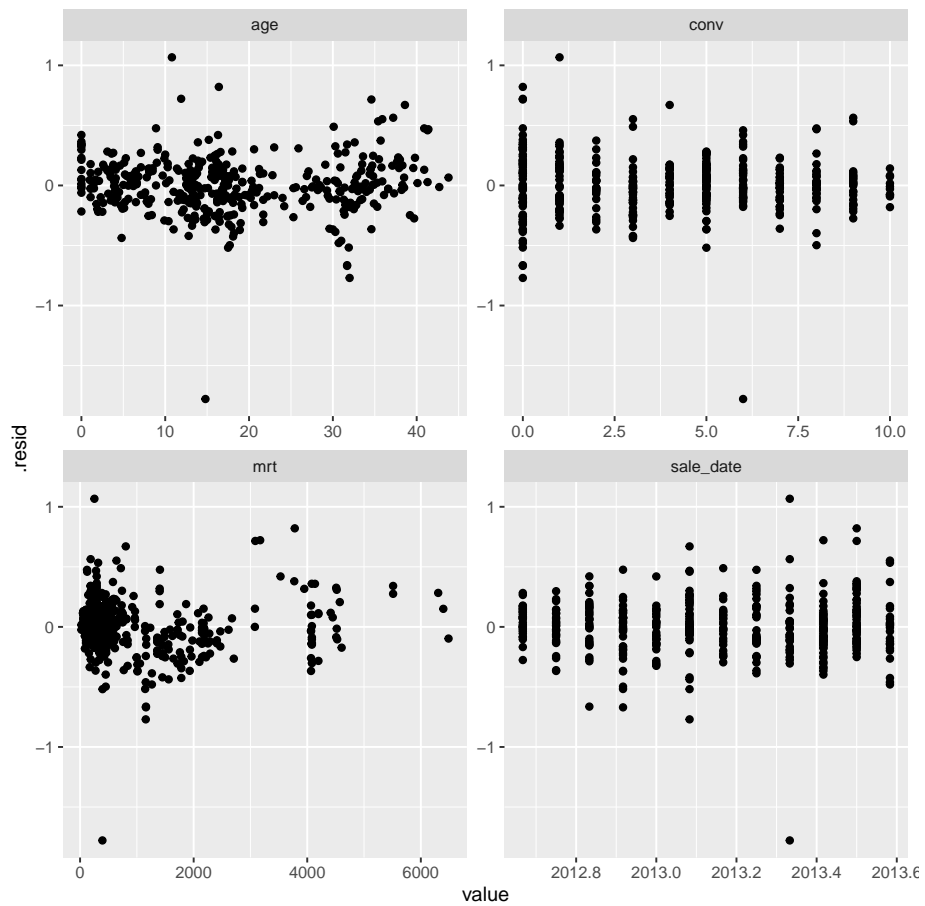


Figure 18: Taiwan houses residual plot 3

```
tibble(x = seq(0, 1, 0.01)) %>%  
  mutate(dens = dgamma(x, 4.6, 17.2)) %>%  
  ggplot(aes(x = x, y = dens)) + geom_line()
```

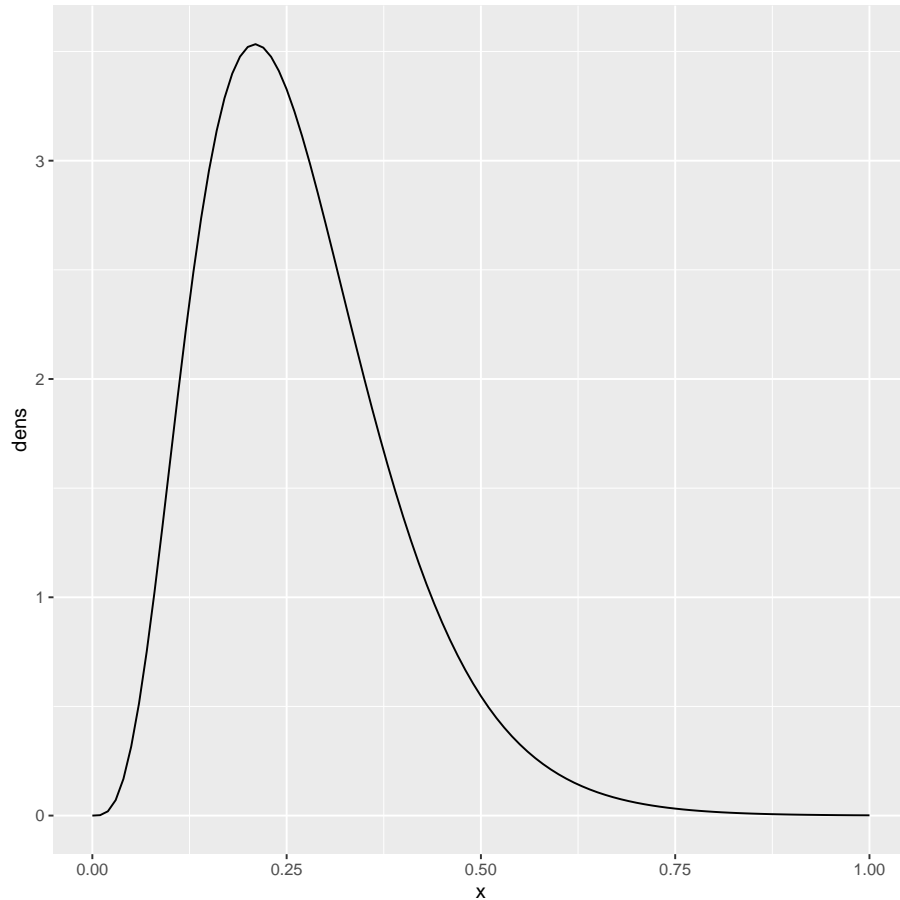


Figure 19: Prior distribution for β

```
my_y <- c(0.5, 0.7, 1.0, 2.5, 7)
```

Figure 20: Data for estimation of β

```
1 / mean(my_y)  
## [1] 0.4273504
```

Figure 21: Maximum likelihood estimate of β

```
expo_fit
## variable mean median sd mad q5 q95 rhat ess_bulk ess_tail
## lp__ -20.70 -20.43 0.70 0.35 -22.23 -20.18 1.00 1834 2319
## beta 0.33 0.32 0.11 0.11 0.18 0.52 1.00 1384 1701
```

Figure 22: Posterior distribution summary