

Booklet of Code and Output  
for  
STAD29/STA 1007 Final Exam

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```

gorilla
##      seen   W   C CW
## 1      0 126 86 64
## 2      0 118 76 54
## 3      0  61 66 44
## 4      0  69 48 32
## 5      0  57 59 42
## 6      0  78 64 53
## 7      0 114 61 41
## 8      0  81 85 47
## 9      0  73 57 33
## 10     0  93 50 45
## 11     0 116 92 49
## 12     0 156 70 45
## 13     0  90 66 48
## 14     0 120 73 49
## 15     0  99 68 44
## 16     0 113 110 47
## 17     0 103 78 52
## 18     0 123 61 28
## 19     0  86 65 42
## 20     0  99 77 51
## 21     0 102 77 54
## 22     0 120 74 53
## 23     0 128 100 56
## 24     0 100 89 56
## 25     0  95 61 37
## 26     0  80 55 36
## 27     0  98 92 51
## 28     0 111 90 52
## 29     0 101 85 45
## 30     0 102 78 51
## 31     1 100 66 48
## 32     1 112 78 55
## 33     1  82 84 37
## 34     1  72 63 46
## 35     1  72 65 47
## 36     1  89 71 49
## 37     1 108 46 29
## 38     1  88 70 49
## 39     1 116 83 67
## 40     1 100 69 39
## 41     1  99 70 43
## 42     1  93 63 36
## 43     1 100 93 62
## 44     1 110 76 56
## 45     1 100 83 36
## 46     1 106 71 49
## 47     1 115 112 66
## 48     1 120 87 54
## 49     1  97 82 41

```

Figure 1: Gorilla and Stroop word test data

```

gorilla.0=glm(seen~1,data=gorilla,family="binomial")
gorilla.1=glm(seen~W+C+CW,data=gorilla,family="binomial")
summary(gorilla.1)

##
## Call:
## glm(formula = seen ~ W + C + CW, family = "binomial", data = gorilla)
##
## Deviance Residuals:
##      Min       1Q   Median       3Q      Max
## -1.0928  -1.0129  -0.9302   1.3330   1.6281
##
## Coefficients:
##              Estimate Std. Error z value Pr(>|z|)
## (Intercept) -0.755980   1.968679  -0.384   0.701
## W           -0.009506   0.018147  -0.524   0.600
## C             0.007602   0.027876   0.273   0.785
## CW            0.014361   0.044204   0.325   0.745
##
## (Dispersion parameter for binomial family taken to be 1)
##
##      Null deviance: 65.438  on 48  degrees of freedom
## Residual deviance: 64.946  on 45  degrees of freedom
## AIC: 72.946
##
## Number of Fisher Scoring iterations: 4

anova(gorilla.0,gorilla.1)

## Analysis of Deviance Table
##
## Model 1: seen ~ 1
## Model 2: seen ~ W + C + CW
##   Resid. Df Resid. Dev Df Deviance
## 1         48     65.438
## 2         45     64.946  3  0.49144

```

Figure 2: Logistic regression for gorilla data

```
boxplot(CW~seen,data=gorilla)
```

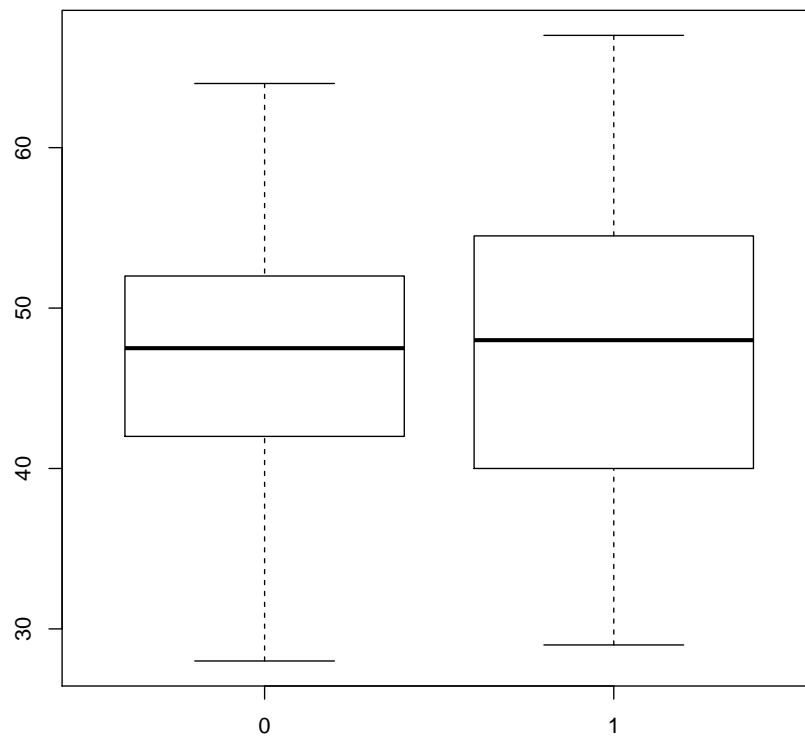


Figure 3: Boxplot of Stroop colour-and-word scores by whether or not gorilla seen

```

autos=read.table("autos.txt",header=T)
head(autos,n=20)

##           make price mpg rep78 headroom trunk weight length turn
## 1      AMC Concord 4099 22     3      2.5   11  2930   186   40
## 2      AMC Pacer  4749 17     3      3.0   11  3350   173   40
## 3      AMC Spirit 3799 22    NA      3.0   12  2640   168   35
## 4    Buick Century 4816 20     3      4.5   16  3250   196   40
## 5    Buick Electra 7827 15     4      4.0   20  4080   222   43
## 6    Buick LeSabre 5788 18     3      4.0   21  3670   218   43
## 7      Buick Opel 4453 26    NA      3.0   10  2230   170   34
## 8      Buick Regal 5189 20     3      2.0   16  3280   200   42
## 9    Buick Riviera 10372 16     3      3.5   17  3880   207   43
## 10   Buick Skylark 4082 19     3      3.5   13  3400   200   42
## 11   Cad. Deville 11385 14     3      4.0   20  4330   221   44
## 12   Cad. Eldorado 14500 14     2      3.5   16  3900   204   43
## 13   Cad. Seville 15906 21     3      3.0   13  4290   204   45
## 14   Chev. Chevette 3299 29     3      2.5    9  2110   163   34
## 15   Chev. Impala  5705 16     4      4.0   20  3690   212   43
## 16   Chev. Malibu  4504 22     3      3.5   17  3180   193   31
## 17 Chev. Monte Carlo 5104 22     2      2.0   16  3220   200   41
## 18   Chev. Monza  3667 24     2      2.0    7  2750   179   40
## 19   Chev. Nova  3955 19     3      3.5   13  3430   197   43
## 20   Dodge Colt  3984 30     5      2.0    8  2120   163   35
## displacement gear_ratio
## 1           121      3.58
## 2           258      2.53
## 3           121      3.08
## 4           196      2.93
## 5           350      2.41
## 6           231      2.73
## 7           304      2.87
## 8           196      2.93
## 9           231      2.93
## 10          231      3.08
## 11          425      2.28
## 12          350      2.19
## 13          350      2.24
## 14          231      2.93
## 15          250      2.56
## 16          200      2.73
## 17          200      2.73
## 18          151      2.73
## 19          250      2.56
## 20          98      3.54

```

Figure 4: 1978 cars data (some)

```

library(MASS)
repf=ordered(autos$rep78)
autos.1=polr(repf~price+mpg+headroom+trunk+weight+length+turn+
  displacement+gear_ratio,data=autos)
autos.2=polr(repf ~ price + mpg + length + turn + displacement,
  data = autos)
anova(autos.2,autos.1)

## Likelihood ratio tests of ordinal regression models
##
## Response: repf
##
## 1 price + mpg + length + turn + displacement Model
## 2 price + mpg + headroom + trunk + weight + length + turn + displacement + gear_ratio
## Resid. df Resid. Dev Test Df LR stat. Pr(Chi)
## 1 60 158.0758
## 2 56 156.5030 1 vs 2 4 1.572858 0.813662

```

Figure 5: Cars fitted models

```

prices=c(4000,6000)
mpgs=20
lengths=200
turns=c(35,45)
displacements=200
new=expand.grid(price=prices,mpg=mpgs,length=lengths,turn=turns,
  displacement=displacements)
pp=predict(autos.2,new,type="p")
cbind(new,pp)

## price mpg length turn displacement 1 2 3
## 1 4000 20 200 35 200 0.003569743 0.01942962 0.2391378
## 2 6000 20 200 35 200 0.002311087 0.01268201 0.1718085
## 3 4000 20 200 45 200 0.055555939 0.22322005 0.5748827
## 4 6000 20 200 45 200 0.036641509 0.16331294 0.5904809
## 4 5
## 1 0.4359874 0.30187542
## 2 0.4124494 0.40074898
## 3 0.1206823 0.02565910
## 4 0.1704300 0.03913469

```

Figure 6: Predictions of repair record for cars data

```

gbcs=read.table("gbcs.txt",header=T)
str(gbcs)

## 'data.frame': 686 obs. of 16 variables:
## $ id          : int  1 2 3 4 5 6 7 8 9 10 ...
## $ diagdateb   : Factor w/ 525 levels "1984-04-25","1984-05-
## 29",...: 21 93 38 9 10 14 109 29 43 106 ...
## $ recdate     : Factor w/ 494 levels "1984-11-24","1985-01-
## 18",...: 151 211 149 1 240 268 27 365 454 471 ...
## $ deathdate   : Factor w/ 471 levels "1984-11-24","1985-03-
## 08",...: 284 275 117 1 174 200 16 390 423 440 ...
## $ age         : int  38 52 47 40 64 49 53 61 43 74 ...
## $ menopause   : int  1 1 1 1 2 2 2 2 1 2 ...
## $ hormone     : int  1 1 1 1 2 2 1 2 1 2 ...
## $ size        : int  18 20 30 24 19 56 52 22 30 20 ...
## $ grade       : int  3 1 2 1 2 1 2 2 2 2 ...
## $ nodes       : int  5 1 1 3 1 3 9 2 1 1 ...
## $ prog_recp   : int  141 78 422 25 19 356 6 6 22 462 ...
## $ estrg_recp  : int  105 14 89 11 9 64 29 173 0 240 ...
## $ rectime     : int  1337 1420 1279 148 1863 1933 358 2372 2563 2372 ...
## $ censrec     : int  1 1 1 0 0 0 1 1 0 0 ...
## $ survtime    : int  2282 2006 1456 148 1863 1933 416 2556 2563 2372 ...
## $ censdead    : int  0 0 1 0 0 0 1 0 0 0 ...

```

Figure 7: Breast cancer data



```

attach(gbcs)
library(survival)
y=Surv(rectime,censrec==1)
y.1=coxph(y~hormone+size+nodes)
summary(y.1)

## Call:
## coxph(formula = y ~ hormone + size + nodes)
##
## n= 686, number of events= 299
##
##              coef exp(coef) se(coef)      z Pr(>|z|)
## hormone -0.364145  0.694790  0.125258 -2.907  0.00365 **
## size      0.007426  1.007454  0.003854  1.927  0.05399 .
## nodes     0.052367  1.053763  0.007319  7.155  8.39e-13 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
##              exp(coef) exp(-coef) lower .95 upper .95
## hormone    0.6948      1.4393    0.5435    0.8881
## size        1.0075      0.9926    0.9999    1.0151
## nodes       1.0538      0.9490    1.0388    1.0690
##
## Concordance= 0.657 (se = 0.016 )
## Likelihood ratio test= 62.02 on 3 df,  p=2e-13
## Wald test               = 87.73 on 3 df,  p=<2e-16
## Score (logrank) test = 90.83 on 3 df,  p=<2e-16

```

Figure 8: Cox modelling of recurrence time

```

hormones=c(1,2)
sizes=c(20,35)
nodeses=c(1,7)
new=expand.grid(hormone=hormones,size=sizes,nodes=nodeses)
pp=survfit(y.1,new)

```

Figure 9: “Survfit”

```
combo=apply(new,1,paste,collapse="-")
combo

## [1] "1-20-1" "2-20-1" "1-35-1" "2-35-1" "1-20-7" "2-20-7" "1-
35-7" "2-35-7"

v=data.frame(time=pp$time,surv=pp$surv)
names(v)=c("time",combo)
library(tidyr)

## Warning: package 'tidyr' was built under R version 3.5.3

p=gather(v,combo,surv,-time)
```

Figure 10: Code for making a ggplot of survival curves

```
library(ggplot2)

## Warning: package 'ggplot2' was built under R version 3.5.3

ggplot(p,aes(x=time,y=surv,colour=combo))+geom_point()+geom_line()
```

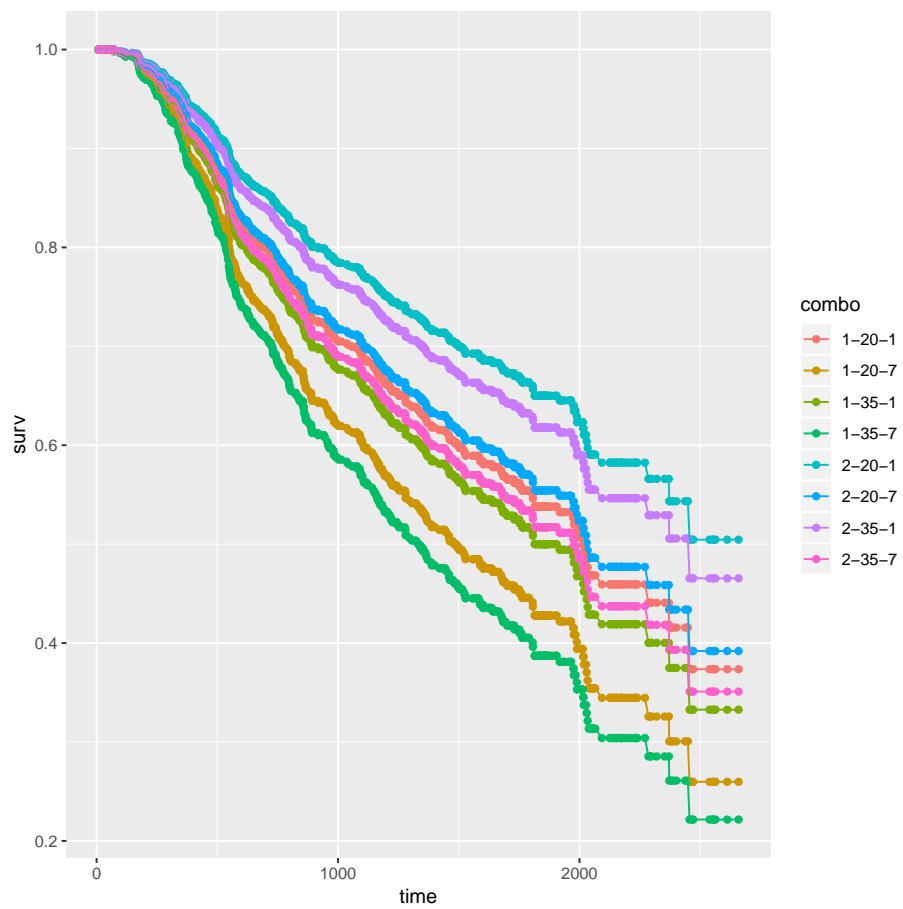


Figure 11: Plot of survival curves

```
french=read.table("learning-french.txt",header=T)
french

##      student book test  gpa
## 1         1    a   34 3.24
## 2         2    a   56 3.44
## 3         3    a   64 3.54
## 4         4    a   69 3.59
## 5         5    a   77 3.65
## 6         6    b   46 3.28
## 7         7    b   61 3.43
## 8         8    b   66 3.48
## 9         9    b   75 3.58
## 10        10    b   77 3.63
## 11        11    c   59 3.35
## 12        12    c   61 3.39
## 13        13    c   72 3.47
## 14        14    c   76 3.52
## 15        15    c   84 3.62
```

Figure 12: French learning data

```
french.1=avov(test~book,data=french)
summary(french.1)

##           Df Sum Sq Mean Sq F value Pr(>F)
## book         2  270.5   135.3   0.759  0.489
## Residuals   12 2137.2   178.1
```

Figure 13: Analysis of variance of test score by book

```
library(ggplot2)
ggplot(french, aes(x=gpa, y=test, colour=book)) +
  geom_point()
```

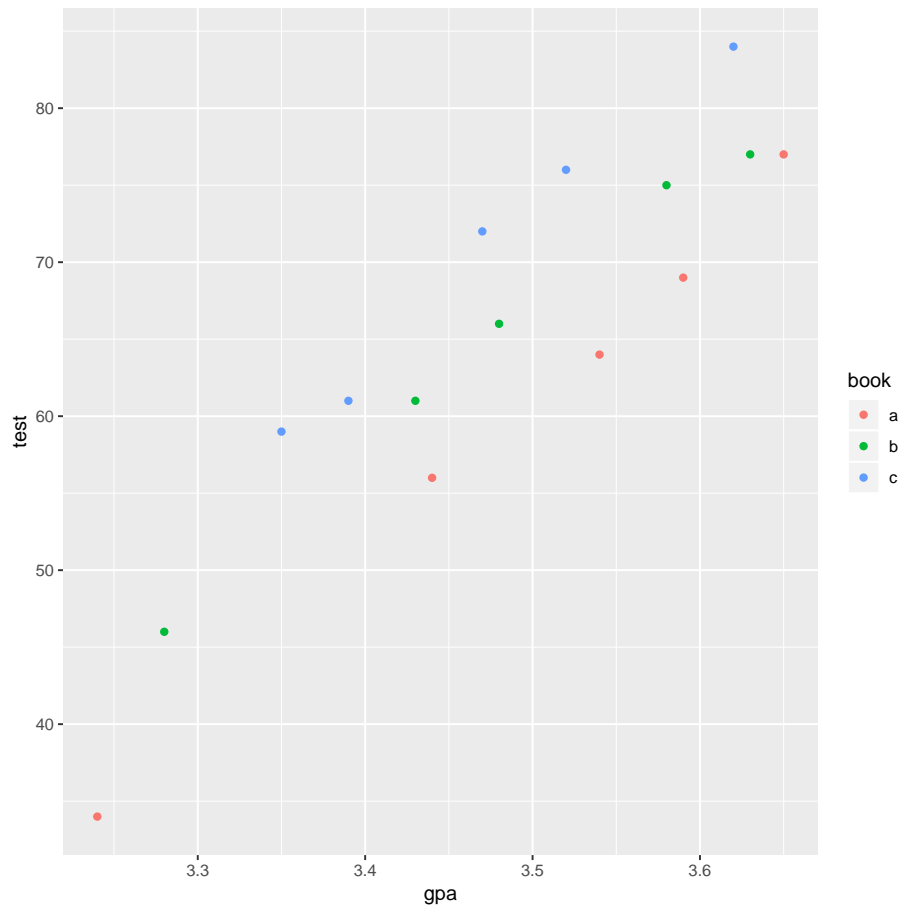


Figure 14: Scatter plot of test score against GPA labelled by textbook

```

french.2=lm(test~gpa*book,data=french)
anova(french.2)

## Analysis of Variance Table
##
## Response: test
##          Df Sum Sq Mean Sq  F value    Pr(>F)
## gpa       1 1994.55 1994.55 1081.2054 1.095e-10 ***
## book      2  390.95  195.47  105.9621 5.559e-07 ***
## gpa:book   2    5.64    2.82    1.5275  0.2684
## Residuals 9   16.60    1.84
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

french.3=update(french.2,.-gpa:book)
anova(french.3)

## Analysis of Variance Table
##
## Response: test
##          Df Sum Sq Mean Sq F value    Pr(>F)
## gpa       1 1994.55 1994.55 986.583 4.044e-12 ***
## book      2  390.95  195.47  96.689 1.048e-07 ***
## Residuals 11   22.24    2.02
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

summary(french.3)

##
## Call:
## lm(formula = test ~ gpa + book, data = french)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -2.5792 -0.8223  0.2805  0.9299  1.6432
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept) -279.4047    10.5128  -26.578 2.48e-11 ***
## gpa          97.1949     3.0050   32.344 2.94e-12 ***
## bookb        6.1663     0.9000    6.852 2.76e-05 ***
## bookc       12.5383     0.9017   13.905 2.52e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.422 on 11 degrees of freedom
## Multiple R-squared:  0.9908, Adjusted R-squared:  0.9882
## F-statistic: 393.3 on 3 and 11 DF, p-value: 1.816e-11

```

Figure 15: Analysis of covariance of test score by book and gpa

```

selfesteem=read.table("therapy.txt",header=T)
selfesteem

##      subject  therapy w1 w2 w3 w4
## 1         1 baseline  3  5  9  6
## 2         2 baseline  7 11 12 11
## 3         3 baseline  9 13 14 12
## 4         4 baseline  4  8 11  7
## 5         5 baseline  1  3  5  4
## 6         6      new   5  6 11  7
## 7         7      new  10 12 18 15
## 8         8      new  10 15 15 14
## 9         9      new   6  9 13  9
## 10        10      new   3  5  9  7

```

Figure 16: Self-esteem therapy data

```

attach(selfesteem)
response=cbind(w1,w2,w3,w4)
selfesteem.1=lm(response~therapy)
library(car)

## Warning: package 'car' was built under R version 3.5.1
## Loading required package: carData
## Warning: package 'carData' was built under R version 3.5.1

weeks=colnames(response)
weeks.df=data.frame(weeks)
selfesteem.2=Manova(selfesteem.1,idata=weeks.df,idesign=~weeks)
selfesteem.2

##
## Type II Repeated Measures MANOVA Tests: Pillai test statistic
##              Df test stat approx F num Df den Df    Pr(>F)
## (Intercept)   1  0.88773   63.259     1     8 4.554e-
05 ***
## therapy       1  0.10886    0.977     1     8   0.3518
## weeks        1  0.98033   99.659     3     6 1.653e-
05 ***
## therapy:weeks 1  0.25600    0.688     3     6   0.5915
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Figure 17: Repeated measures analysis for therapy data

```
library(tidyr)
selfesteem.long=gather(selfesteem,weeks,self.esteem,w1:w4)
```

Figure 18: Reorganizing the therapy data

```
ggplot(selfesteem.long,
aes(x=weeks,y=self.esteem,
group=subject,colour=therapy)) + geom_line()
```

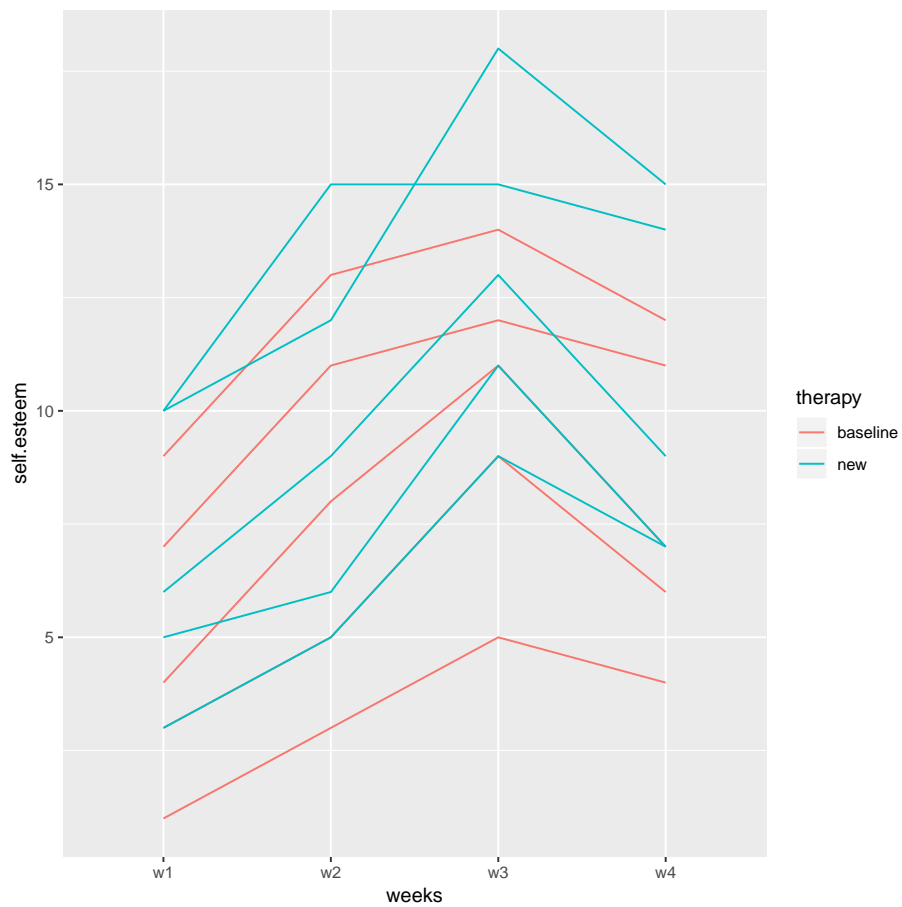


Figure 19: Spaghetti plot for therapy data



```

mags=read.table("MAGAZINES.txt",header=T)
str(mags)

## 'data.frame': 141 obs. of 16 variables:
## $ id      : int  101 102 103 104 105 106 107 108 109 110 ...
## $ magazine : int  4 3 2 4 4 2 1 3 4 2 ...
## $ i1      : int  0 0 0 0 0 0 1 0 0 0 ...
## $ i2      : int  0 0 1 0 0 1 0 0 0 1 ...
## $ i3      : int  0 1 0 0 0 0 0 1 0 0 ...
## $ i4      : int  1 0 0 1 1 0 0 0 1 0 ...
## $ famsize  : int  2 2 1 1 2 1 2 1 1 4 ...
## $ income   : int  11 11 8 11 10 6 11 1 6 4 ...
## $ race     : int  1 1 1 1 1 1 1 0 1 0 ...
## $ tv       : int  3 2 1 1 2 1 3 3 2 2 ...
## $ newspaper: int  1 1 0 1 1 1 1 0 0 0 ...
## $ nomale   : int  0 0 1 1 0 1 0 1 1 0 ...
## $ nofemale : int  0 0 0 0 0 0 0 0 0 0 ...
## $ child18  : int  1 1 1 1 1 1 1 1 1 0 ...
## $ headage  : int  6 5 6 5 6 6 5 5 5 3 ...
## $ headeduc : int  7 7 4 6 6 5 7 3 6 5 ...

```

Figure 20: Summary of magazine data

```

library(MASS)
mags.1=lda(magazine~famsize+income+race+tv+newspaper+nomale+
           nofemale+child18+headage+headeduc,data=mags)
mags.1

## Call:
## lda(magazine ~ famsize + income + race + tv + newspaper + nomale +
##      nofemale + child18 + headage + headeduc, data = mags)
##
## Prior probabilities of groups:
##      1          2          3          4
## 0.1843972 0.3475177 0.2765957 0.1914894
##
## Group means:
##   famsize  income      race      tv newspaper  nomale  nofemale
## 1 2.730769 7.384615 0.8846154 2.000000 0.4615385 0.1538462 0.0000000
## 2 2.163265 4.897959 0.7142857 1.734694 0.3877551 0.5510204 0.06122449
## 3 2.102564 5.333333 0.6923077 1.794872 0.2564103 0.3846154 0.10256410
## 4 2.074074 8.370370 0.8518519 1.703704 0.5185185 0.3703704 0.18518519
##   child18  headage  headeduc
## 1 0.7307692 4.692308 5.500000
## 2 0.7755102 5.061224 4.775510
## 3 0.7435897 4.589744 5.000000
## 4 0.8148148 4.444444 6.185185
##
## Coefficients of linear discriminants:
##           LD1          LD2          LD3
## famsize  -0.02506254  0.31004546  0.99557640
## income   -0.26488338  0.04896005  0.03142841
## race      0.02724269 -0.82876993  0.60290221
## tv        0.34729706  0.01278338 -0.22388539
## newspaper 0.12958772  0.55766570  0.97724506
## nomale   -0.06306391  2.70594323  1.26670569
## nofemale -0.58564087  3.10963239  0.14905016
## child18  -0.75018974 -0.14545284  1.07604018
## headage   0.23540594  0.03287999  0.52175803
## headeduc -0.27938790  0.10107380  0.01459669
##
## Proportion of trace:
##   LD1  LD2  LD3
## 0.5715 0.2739 0.1546

```

Figure 21: Discriminant analysis for magazine data

```
plot(mags.1,dimen=2,col=mags$magazine)
```

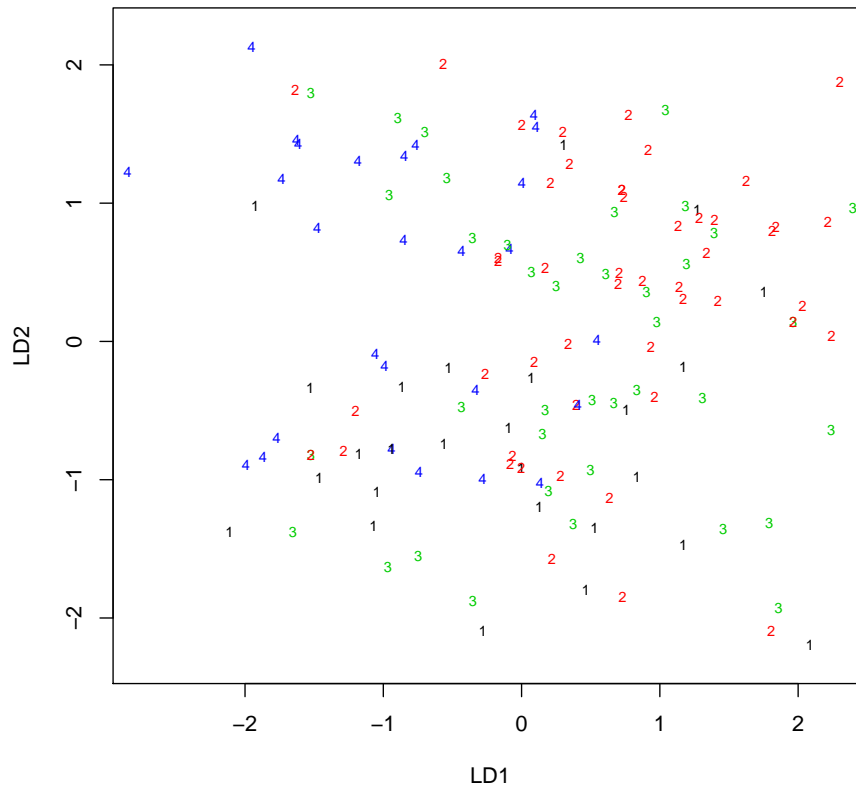


Figure 22: Plot of first two discriminant scores for magazine data

```
pp=predict(mags.1)  
table(magazine=mags$magazine,predicted=pp$class)
```

```
##           predicted  
## magazine  1  2  3  4  
##           1 10  8  5  3  
##           2  8 32  7  2  
##           3  4 16 14  5  
##           4  4  6  2 15
```

Figure 23: Predictions for magazine data

```

set.seed(457299)
post=round(pp$posterior,3)
row=sample(nrow(post),10)
cbind(mags[row,],guess=pp$class[row],post[row,])

```

##	id	magazine	i1	i2	i3	i4	famsize	income	race	tv	newspaper	nomale	
##	134	234	2	0	1	0	0	2	11	1	2	1	0
##	18	118	4	0	0	0	1	4	8	1	3	0	0
##	32	132	1	1	0	0	0	4	9	1	2	1	0
##	77	177	3	0	0	1	0	1	11	1	3	1	1
##	54	154	1	1	0	0	0	4	7	1	1	0	0
##	103	203	4	0	0	0	1	2	11	1	1	1	0
##	33	133	4	0	0	0	1	4	11	1	2	1	0
##	30	130	3	0	0	1	0	4	6	0	2	0	0
##	78	178	2	0	1	0	0	1	5	1	1	0	1
##	110	210	1	1	0	0	0	1	4	0	1	0	1

##	nofemale	child18	headage	headeduc	guess	1	2	3	4	
##	134	0	1	5	7	1	0.393	0.100	0.129	0.378
##	18	0	1	5	6	1	0.468	0.256	0.156	0.120
##	32	0	0	4	7	2	0.287	0.293	0.182	0.238
##	77	0	1	6	6	4	0.075	0.367	0.110	0.447
##	54	0	0	3	4	3	0.325	0.205	0.394	0.075
##	103	0	1	5	7	4	0.384	0.074	0.090	0.452
##	33	0	0	4	7	4	0.276	0.207	0.137	0.379
##	30	0	1	6	4	2	0.257	0.500	0.187	0.057
##	78	0	1	5	6	2	0.118	0.354	0.299	0.230
##	110	0	1	6	6	2	0.050	0.487	0.291	0.172

Figure 24: Sample of posterior probabilities

```

cars=read.csv("CAR_DISSIM.csv",header=T,stringsAsFactors=F)
cars

```

##	Car	BMW	Ford	Infnti	Jeep	Lexus	Chrys	Merc	Saab	Porsche	Volvo
##	1	BMW	0	NA	NA	NA	NA	NA	NA	NA	NA
##	2	Ford	34	0	NA	NA	NA	NA	NA	NA	NA
##	3	Infiniti	8	24	0	NA	NA	NA	NA	NA	NA
##	4	Jeep	31	2	25	0	NA	NA	NA	NA	NA
##	5	Lexus	7	26	1	27	0	NA	NA	NA	NA
##	6	Chrysler	43	14	35	15	37	0	NA	NA	NA
##	7	Mercedes	3	28	5	29	4	42	0	NA	NA
##	8	Saab	10	18	20	17	13	36	19	0	NA
##	9	Porsche	6	39	41	38	40	45	32	21	0
##	10	Volvo	33	11	22	12	23	9	30	16	44

Figure 25: Cars data for multidimensional scaling

```
d=as.dist(cars[,-1])
library(MASS)
d.1=isoMDS(d)

## initial value 10.466056
## iter 5 value 6.523088
## iter 10 value 4.865126
## iter 15 value 4.088399
## iter 20 value 4.003118
## final value 3.989006
## converged

d.1$stress

## [1] 3.989006
```

Figure 26: Multidimensional scaling analysis of cars

```
plot(d.1$points,xlim=c(-30,30))
text(d.1$points,cars$Car,pos=4)
```

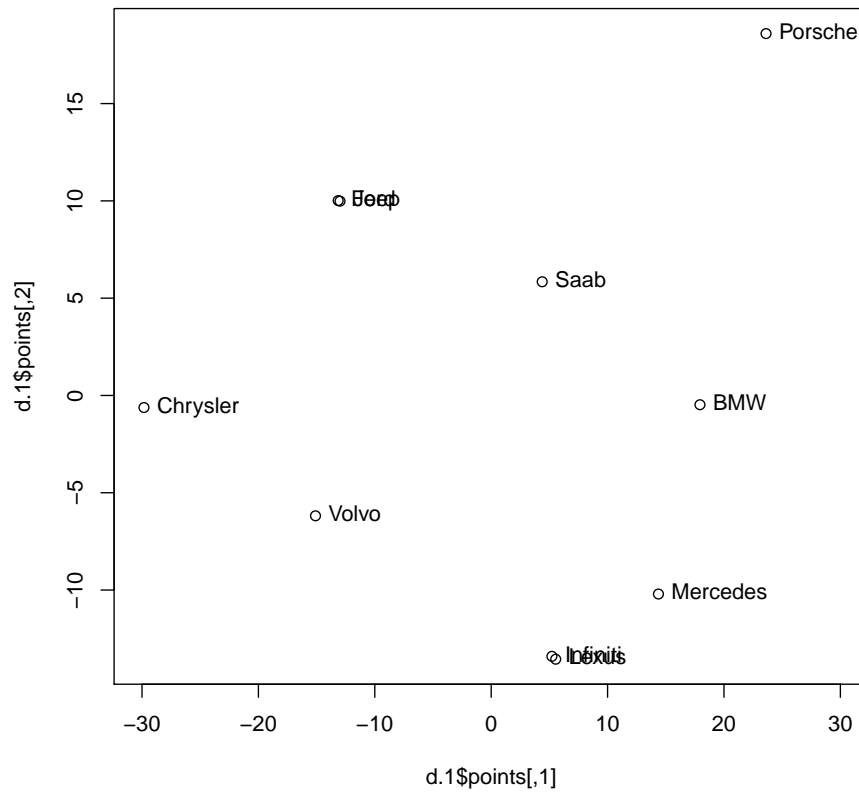


Figure 27: Multidimensional scaling map of cars

```
## Warning: package 'dplyr' was built under R version 3.5.2
```

```
baseball

##           TEAM  RS    H  HR  AVG    W  ERA  RA    SO  BB  E
## 1      Toronto 891 1480 232 0.269  93 3.80 670 1117 397 88
## 2    NY Yankees 764 1397 212 0.251  87 4.05 698 1370 474 92
## 3         Texas 751 1419 172 0.257  88 4.24 733 1095 508 119
## 4         Boston 748 1496 161 0.265  78 4.31 753 1218 478 97
## 5         Colorado 737 1479 186 0.265  68 5.04 844 1112 579 95
## 6         Houston 729 1363 230 0.250  86 3.57 618 1280 423 85
## 7    Kansas City 724 1497 139 0.269  95 3.73 641 1160 489 88
## 8         Arizona 720 1494 154 0.264  79 4.04 713 1215 500 86
## 9         Baltimore 713 1370 217 0.250  81 4.05 693 1233 483 77
## 10    Washington 703 1363 177 0.251  83 3.62 635 1342 364 90
## 11    Pittsburgh 697 1462 140 0.260  98 3.21 596 1338 453 122
## 12 San Francisco 696 1486 136 0.267  84 3.72 627 1165 431 78
## 13         Minnesota 696 1349 156 0.247  83 4.07 700 1046 413 86
## 14         Oakland 694 1405 146 0.251  68 4.14 729 1179 474 126
## 15         Detroit 689 1515 151 0.270  74 4.64 803 1100 489 86
## 16 Chicago Cubs 689 1341 171 0.244  97 3.36 608 1431 407 111
## 17         NY Mets 683 1351 177 0.244  90 3.43 613 1337 383 88
## 18         Cleveland 669 1395 141 0.256  81 3.67 640 1407 425 79
## 19    LA Dodgers 667 1346 187 0.250  92 3.44 595 1396 395 75
## 20    LA Angels 661 1331 176 0.246  85 3.94 675 1221 466 93
## 21         Seattle 656 1379 198 0.249  76 4.16 726 1283 491 94
## 22         Milwaukee 655 1378 145 0.251  68 4.28 737 1260 517 116
## 23         San Diego 650 1324 148 0.243  74 4.09 731 1393 516 92
## 24         St. Louis 647 1386 137 0.253 100 2.94 525 1329 477 96
## 25         Tampa Bay 644 1383 167 0.252  80 3.74 642 1355 477 95
## 26         Cincinnati 640 1382 167 0.248  64 4.33 754 1252 544 90
## 27 Philadelphia 626 1374 130 0.249  63 4.69 809 1153 488 117
## 28 Chicago Sox 622 1381 136 0.250  76 3.98 701 1359 474 101
## 29         Miami 613 1420 120 0.260  71 4.02 678 1152 508 77
## 30         Atlanta 573 1361 100 0.251  67 4.41 760 1148 550 90
```

Figure 28: Baseball data

```

baseball.1=princomp(baseball[,-1],cor=T)
summary(baseball.1)

## Importance of components:
##              Comp.1    Comp.2    Comp.3    Comp.4    Comp.5
## Standard deviation  1.9780942  1.6284703  1.1592964  1.001404  0.72347227
## Proportion of Variance 0.3912857  0.2651916  0.1343968  0.100281  0.05234121
## Cumulative Proportion 0.3912857  0.6564772  0.7908740  0.891155  0.94349624
##              Comp.6    Comp.7    Comp.8    Comp.9
## Standard deviation  0.58886348  0.33939375  0.269085919  0.158853043
## Proportion of Variance 0.03467602  0.01151881  0.007240723  0.002523429
## Cumulative Proportion 0.97817226  0.98969108  0.996931800  0.999455229
##              Comp.10
## Standard deviation  0.0738086322
## Proportion of Variance 0.0005447714
## Cumulative Proportion 1.0000000000

```

Figure 29: Principal components analysis of baseball data



```
plot(baseball.1,type="l")
```

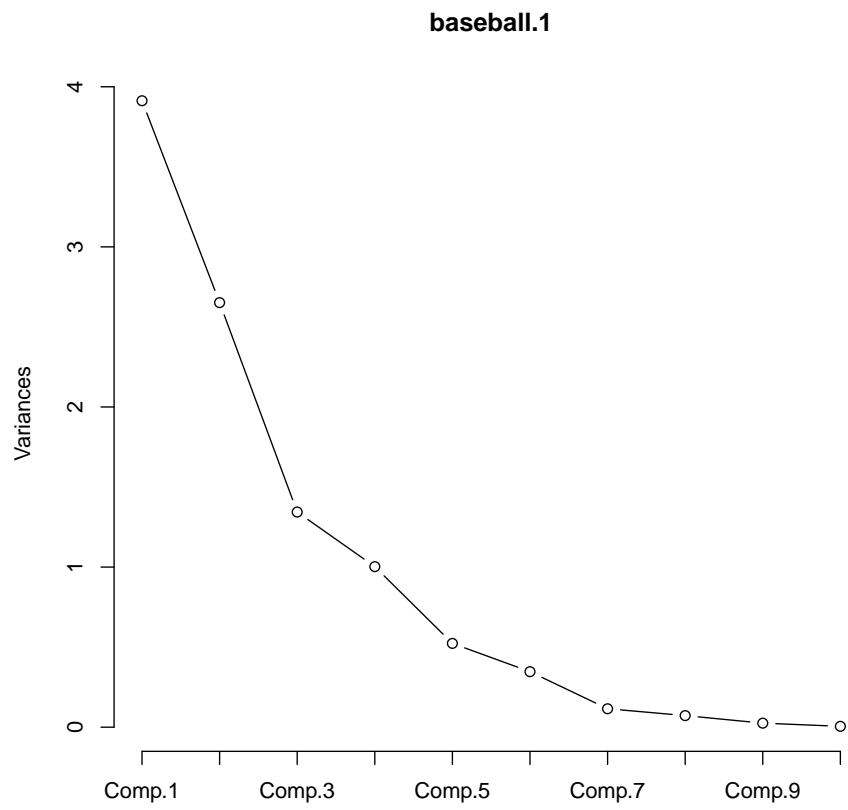


Figure 30: Scree plot of baseball data

```

baseball.2=factanal(baseball[,-1],4,scores="r")
baseball.2$uniquenesses

##          RS          H          HR          AVG          W          ERA
## 0.00500000 0.03362356 0.24671588 0.00500000 0.16953992 0.00500000
##          RA          SO          BB          E
## 0.00500000 0.47513335 0.41234633 0.48432288

baseball.2$PVAL

## objective
## 0.3670648

baseball.2$loadings

##
## Loadings:
##      Factor1 Factor2 Factor3 Factor4
## RS  -0.131   0.480   0.861
## H    0.113   0.975
## HR           -0.125   0.846  -0.117
## AVG           0.984           -0.141
## W   -0.851   0.134   0.297
## ERA  0.989   0.121
## RA   0.977   0.108           0.171
## SO  -0.538  -0.449  -0.112   0.148
## BB   0.666   0.134  -0.342
## E                0.707
##
##              Factor1 Factor2 Factor3 Factor4
## SS loadings      3.441   2.434   1.680   0.604
## Proportion Var   0.344   0.243   0.168   0.060
## Cumulative Var   0.344   0.587   0.755   0.816

```

Figure 31: Factor analysis for baseball data

```
biplot(baseball.2$scores,baseball.2$loadings,cex=c(1,0.5))
```

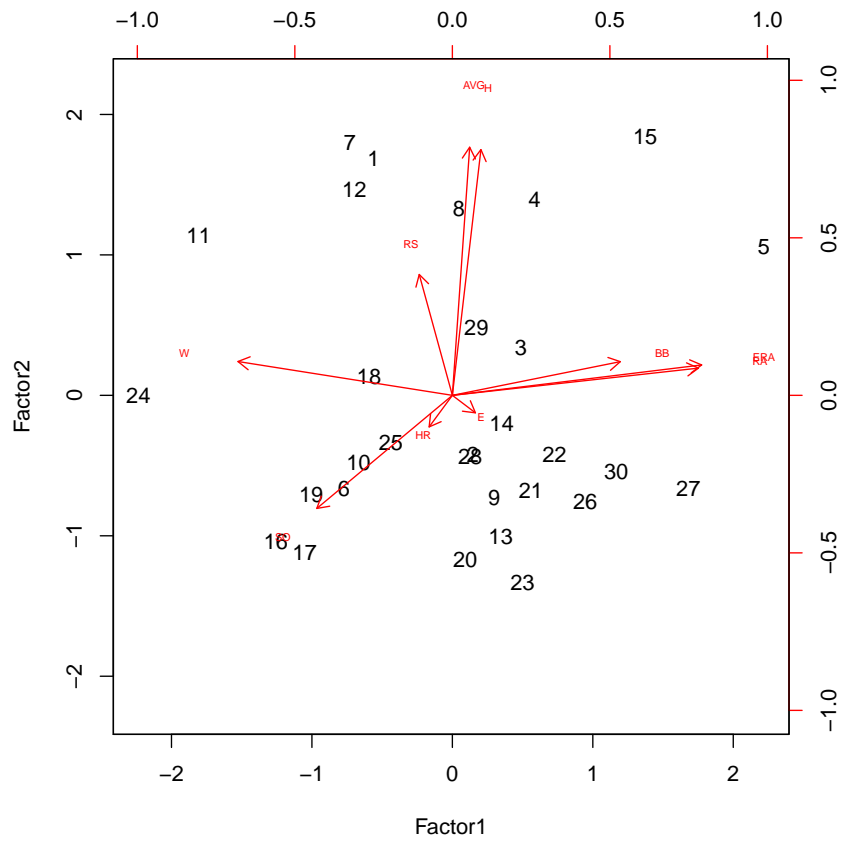


Figure 32: Biplot of baseball factor analysis

```

genders=c("male","female")
ruptures=c("no","yes")
cesareans=c("no","yes")
induced=c("no","yes")
combos=expand.grid(induced=induced,cesarean=cesareans,
                    rupture=ruptures,gender=genders)
freqs=c(177,45,37,18,104,16,9,7,137,53,24,12,74,15,8,2)
births=cbind(combos,freq=freqs)
births

##      induced cesarean rupture gender freq
## 1         no         no      no  male  177
## 2         yes         no      no  male   45
## 3         no         yes      no  male   37
## 4         yes         yes      no  male   18
## 5         no         no       yes  male  104
## 6         yes         no       yes  male   16
## 7         no         yes       yes  male    9
## 8         yes         yes       yes  male    7
## 9         no         no      no female 137
## 10        yes         no      no female  53
## 11        no         yes      no female  24
## 12        yes         yes      no female  12
## 13        no         no       yes female  74
## 14        yes         no       yes female  15
## 15        no         yes       yes female   8
## 16        yes         yes       yes female   2

```

Figure 33: Birth data

```

births.1=glm(freq~gender*rupture*cesarean*induced,data=births,
             family="poisson")
drop1(births.1,test="Chisq")

## Single term deletions
##
## Model:
## freq ~ gender * rupture * cesarean * induced
##
##           Df Deviance    AIC    LRT Pr(>Chi)
## <none>
##           0.00000 113.00
## gender:rupture:cesarean:induced  1  0.83372 111.84 0.83372  0.3612

```

Much analysis follows (not shown).

I ended with:

```

births.10=update(births.9,.-gender:induced)
drop1(births.10,test="Chisq")

## Single term deletions
##
## Model:
## freq ~ gender + rupture + cesarean + induced + rupture:cesarean +
##         rupture:induced + cesarean:induced
##
##           Df Deviance    AIC    LRT Pr(>Chi)
## <none>
##           8.9101 105.91
## gender      1  19.4284 114.43 10.5182 0.001182 **
## rupture:cesarean  1  13.9746 108.98  5.0645 0.024421 *
## rupture:induced  1  14.4372 109.44  5.5271 0.018725 *
## cesarean:induced  1  15.9388 110.94  7.0286 0.008022 **
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Figure 34: Birth data log-linear analysis

```

xt1=xtabs(freq~rupture+cesarean,data=births)
prop.table(xt1,1)

##          cesarean
## rupture      no      yes
##    no  0.8190855 0.1809145
##    yes 0.8893617 0.1106383

xt2=xtabs(freq~rupture+induced,data=births)
prop.table(xt2,1)

##          induced
## rupture      no      yes
##    no  0.7455268 0.2544732
##    yes 0.8297872 0.1702128

xt3=xtabs(freq~cesarean+induced,data=births)
prop.table(xt3,2)

##          induced
## cesarean      no      yes
##    no  0.8631579 0.7678571
##    yes 0.1368421 0.2321429

```

Figure 35: Birth data sub-tables